

# CS122A: Introduction to Data Management

## Lecture #13: Relational DB Design Theory (II)

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# Third Normal Form (3NF)

- ❖ Relation R is in **3NF** if it is in 2NF and it has no *transitive* dependencies to non-prime attributes.

## Violation



# Example

## ❖ Workers(eno, ename, esal, dno, dname, dfloor)

where:  $eno \rightarrow ename$ ,  $eno \rightarrow esal$ ,  $eno \rightarrow dno$ ,  $dno \rightarrow dname$ ,  $dno \rightarrow dfloor$

Q1: What are the candidate keys for Workers?

Q2: What are the prime attributes for Workers?

Q3: Why is Workers not in 3NF?

Q4: What's the fix?

Emp(eno, ename, esal, dno)

Dept(dno, dname, dfloor)

A1: eno

A2: eno

A3: Two inferable FDs,  
 $eno \rightarrow dname$  and  
 $eno \rightarrow dfloor$ , each  
violate 3NF.

Don't forget this!  
(Else “**lossy join**” !!)

# Boyce-Codd Normal Form (BCNF)

- ❖ Rel'n R with FDs  $F$  is in **BCNF** if, for all  $X \rightarrow A$  in  $F^+$ 
  - $A \in X$  (*trivial* FD), or else
  - $X$  is a *superkey* (i.e., contains a key) for R.

Violation

**Not a superkey**

**Not a subset of X**



# *Boyce-Codd Normal Form (BCNF)*

- ❖ R is in BCNF if the *only* non-trivial FDs that hold over R are *key constraints!* (i.e.,  $key \rightarrow attr$ )
  - Everything depends on “**the key, the whole key, and nothing but the key**” (so help me Codd 😊)

# Boyce-Codd Normal Form (Cont'd.)

❖ *Ex:* Supply2(sno, sname, pno)

where: sno  $\rightarrow$  sname, sname  $\rightarrow$  sno

Q1: What are the candidate keys for Supply2?

Q2: What are the prime attributes for Supply2?

Q3: Is Supply2 in 3NF?

Q4: Why is Supply2 not in BCNF?

Q5: What's the fix?

Supplier2(sno, sname)

Supplies2(sno, pno)

*Note: Overlapping...!*

A1: (sno, pno), (sname, pno)

A2: sno, sname, pno

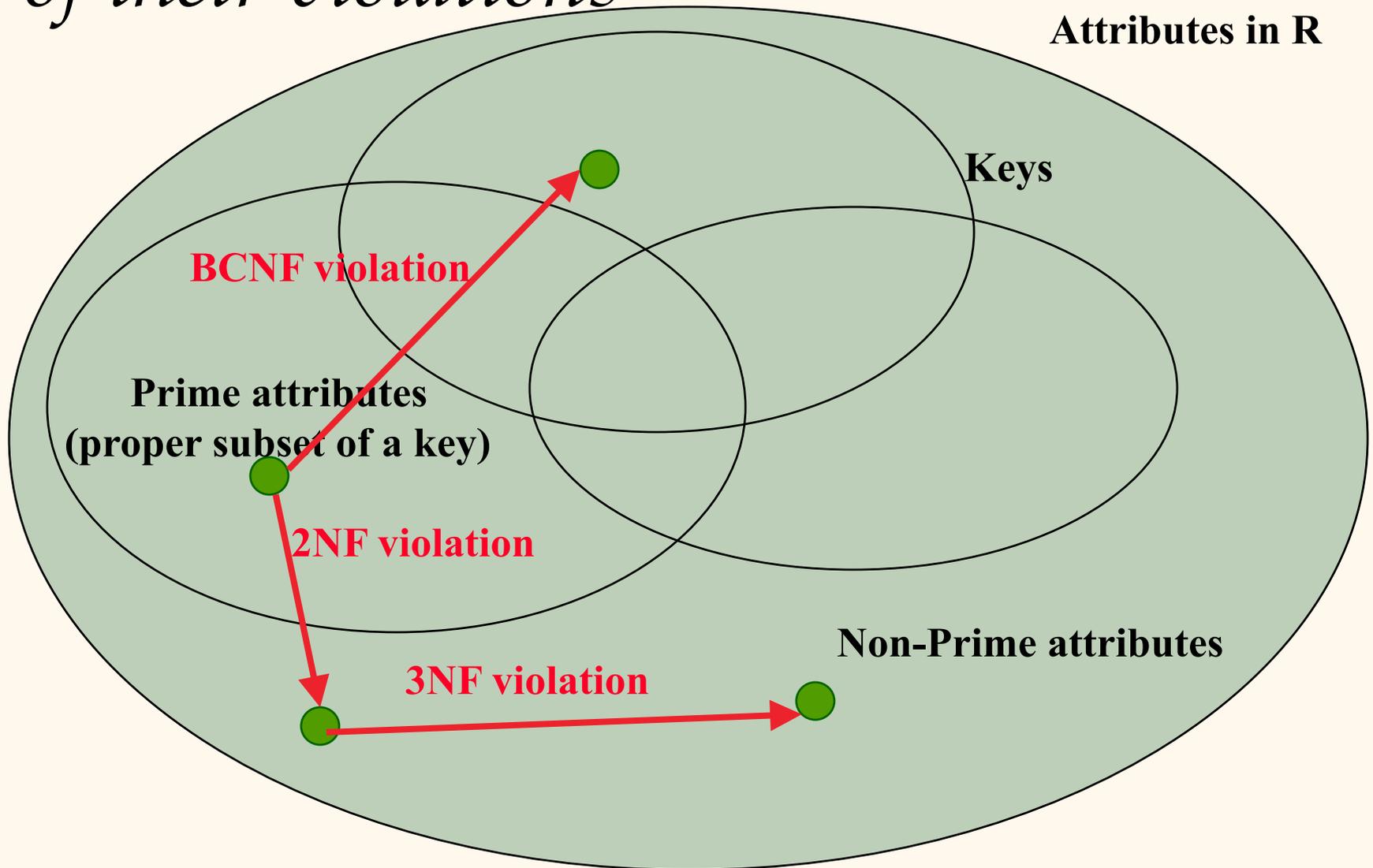
A3: Yes, it is in 3NF.

A4: Each of its FDs has a left-hand-side that isn't a candidate key. (Just a part of one.)

## *3NF Revisited (Alternative Def'n)*

- ❖ Rel'n R with FDs  $F$  is in **3NF** if, for all  $X \rightarrow A$  in  $F^+$ 
  - $A \in X$  (*trivial* FD), or else
  - $X$  is a superkey (i.e., contains a key) for R, or else
  - $A$  is part of some key for R.
- ❖ If R is in BCNF, clearly it is also in 3NF.

# Summary of normal forms (in terms of their violations)



# *Decomposition of a Relation Scheme*

- ❖ Suppose that relation R contains attributes  $A_1 \dots A_n$ . A decomposition of R consists of replacing R by two or more relations such that:
  - Each new relation scheme contains a subset of the attributes of R (and no attributes that do not appear in R ☺), and
  - Every attribute of R appears as an attribute of one of the new relations.
- ❖ Intuitively, decomposing R means we will store instances of the relations produced by the decomposition *instead* of storing instances of R.
- ❖ E.g., decompose **SNLRWH** into **SNLRH** and **RW**.

# Example Decomposition

- ❖ Decompositions should be used only when needed.
  - Suppose **SNLRWH** has 2 FDs: **S** → **SNLRWH** and **R** → **W**
  - Second FD causes violation of 3NF (**W** values repeatedly associated with **R** values). Easiest fix is to create a relation **RW** to store these associations, and then to remove **W** from the main schema:
    - I.e.: Decompose **SNLRWH** into **SNLRH** and **RW**.
- ❖ The information to be stored consists of **SNLRWH** tuples. (If we just store the projections of these tuples onto **SNLRH** and **RW**, are there any potential problems that we should be aware of? ... →)

# Reminder:

Wages

R	W
8	10
5	7

HourlyEmps2

S	N	L	R	H
123-22-3666	Attishoo	48	8	40
231-31-5368	Smiley	22	8	30
131-24-3650	Smethurst	35	5	30
434-26-3751	Guldu	35	5	32
612-67-4134	Madayan	35	8	40

S	N	L	R	W	H
123-22-3666	Attishoo	48	8	10	40
231-31-5368	Smiley	22	8	10	30
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434-26-3751	Guldu	35	5	7	32
612-67-4134	Madayan	35	8	10	40

❖ Problems due to  $R \rightarrow W$  :

- Update anomaly: Can we change  $W$  in just the 1st tuple of SNLRWH?
- Insertion anomaly: What if we want to insert an employee and don't know the hourly wage for his rating?
- Deletion anomaly: If we delete all employees with rating 5, we lose the information about the wage for rating 5!

How about two smaller tables?

# *Decompositions: Possible Problems*

- ❖ There are three potential problems to consider:
  1. **Some queries become more expensive.**
    - E.g., how much did sailor Joe earn? ( $S = W * H$  now requires a join)
  2. **Given instances of the decomposed relations, we may not be able to reconstruct the corresponding instance of the original relation! (If “lossy” ...)**
    - Fortunately, not a problem in the SNLRWH example!
  3. **Checking some dependencies may require joining the instances of the decomposed relations.**
    - Fortunately, also not in the SNLRWH example.
- ❖ **Tradeoff:** Must consider these issues vs. redundancy.

# Lossless Join Decompositions

- ❖ Decomposition of  $\mathbf{R}$  into  $\mathbf{X}$  and  $\mathbf{Y}$  is lossless-join w.r.t. a set of FDs  $F$  if, for every instance  $r$  that satisfies  $F$ :
  - $\pi_X(r) \bowtie \pi_Y(r) = r$
- ❖ It is always true that  $r \subseteq \pi_X(r) \bowtie \pi_Y(r)$ 
  - In general, the other direction does not hold! If it does, then the decomposition is called lossless-join.
  - Must ensure that  $X$  and  $Y$  overlap, and that the overlap contains a key for one of the two relations.
- ❖ Definition extends to decomposition into 3 or more relations in a straightforward way.
- ❖ *Decompositions must be lossless! (Avoids Problem (2).)*

# Decomposition **not** lossless-join (bad)

S	N	L	R	W	H
123-22-3666	Attishoo	48	8	10	40
231-31-5368	Smiley	22	8	10	30
131-24-3650	Smethurst	35	5	7	30
434-26-3751	Guldu	35	5	7	32
612-67-4134	Madayan	35	8	10	40

HourlyEmps3

S	N	L	R	W
123-22-3666	Attishoo	48	8	10
231-31-5368	Smiley	22	8	10
131-24-3650	Smethurst	35	5	7
434-26-3751	Guldu	35	5	7
612-67-4134	Madayan	35	8	10

Hours

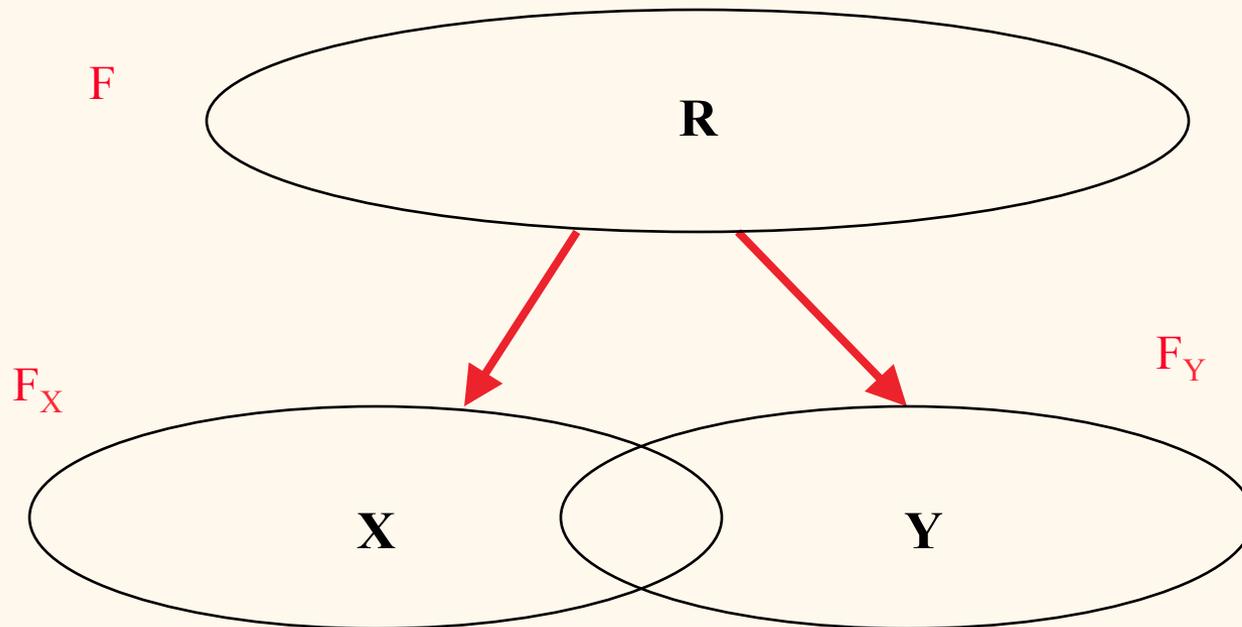
R	H
8	40
8	30
5	30
5	32
8	40

# Dependency Preserving Decomposition

- ❖ Consider CSJDPQV, C is key, JP  $\rightarrow$  C and SD  $\rightarrow$  P.
  - BCNF decomposition: CSJDQV and SDP
  - Problem: Checking JP  $\rightarrow$  C requires a join!
- ❖ **Dependency preserving decomposition** (intuitive):
  - If R is decomposed into X, Y and Z, and we enforce the FDs that hold on X, on Y, and on Z, then all FDs that were given to hold on R must also hold. (Avoids Problem (3).)
- ❖ Projection of set of FDs F: If R is decomposed into X, ... projection of F onto X (denoted  $F_X$ ) is the set of FDs  $U \rightarrow V$  in  $F^+$  (**closure** of F) such that **U, V both in X**.

# Dependency Preserving Decomp. (Cont'd.)

- ❖ Decomposition of  $R$  into  $X$  and  $Y$  is dependency preserving if  $(F_X \text{ union } F_Y)^+ = F^+$ 
  - I.e., if we consider only dependencies in the closure  $F^+$  that can be checked in  $X$  without considering  $Y$ , and in  $Y$  without considering  $X$ , they **imply** all dependencies in  $F^+$ .



# *Dependency Preserving Decomp. (Cont'd.)*

- ❖ Important to consider  $F^+$ , not  $F$ , in this definition:
  - $R(ABC), A \rightarrow B, B \rightarrow C, C \rightarrow A,$
  - 2NF? Yes
  - 3NF? Yes
  - BCNF? **Yes**
  - Decomposed into AB and BC.
  - Is this dependency preserving? (Is  $C \rightarrow A$  preserved?)

# Dependency Preserving Decomp. (Cont'd.)

- ❖ Dependency preserving does *not* imply lossless join:
  - $R(ABC)$ , only  $A \rightarrow B$ ,
  - 2NF? No
  - If decomposed into  $AB$  and  $BC$ .
    - Dependency preserving? Yes.
    - Lossless join? No
- ❖ And vice-versa! (So we need to check for both.)
  - Must make sure **some** relation contains a **key** for  $R$ !!!

# 3NF Revisited

- ❖ If R is in 3NF, some redundancy is possible. 3NF is a compromise to use when BCNF isn't achievable (e.g., no “good” decomp, or performance considerations).
- ❖ Important: *A lossless-join, dependency-preserving decomposition of R into a collection of 3NF relations is **always** possible.*

# BCNF Revisited

Note: A lossless-join, *dependency-preserving* decomposition of  $R$  into a collection of BCNF relations is NOT always possible.

# Summary of normalization theory