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Let the relation  $R(A, B, C, D, E)$  have a functional dependency set  $F = \{A \rightarrow B, B \rightarrow C, CD \rightarrow E\}$ .

1. Suppose we decompose  $R$  into  $R_1(A, B, C)$  and  $R_2(C, D, E)$

a. Compute the local dependencies in  $F_{R_1}$  and  $F_{R_2}$ .

$$F_{R_1} = \{A \rightarrow B, B \rightarrow C\}$$

$$F_{R_2} = \{CD \rightarrow E\}$$

b. What's the strongest normal form of  $R_1$  and  $R_2$  respectively?

**The strongest normal form of  $R_1$  is 2NF ( $R_1$  violates 3NF due to transitivity, ie,  $A \rightarrow B$  and  $B \rightarrow C$  imply  $A \rightarrow C$ ) and  $R_2$  is BCNF (since there is only one dependency  $CD \rightarrow E$ )**

c. Is this decomposition lossless join?

**No, since the  $R_1 \cap R_2 = C$  but  $C$  is a key for neither  $R_1$  nor  $R_2$**

d. Is this decomposition dependency preserving?

**Yes (it is easy to check that  $(F_{R_1} \cup F_{R_2})^+ = F^+$ )**

2. Suppose we decompose  $R$  into  $R_3(A, B, C, D)$ ,  $R_2(C, D, E)$ .

a. Compute the local dependencies in  $F_{R_3}$  and  $F_{R_2}$ .

$$F_{R_3} = \{A \rightarrow B, B \rightarrow C\}$$

$$F_{R_2} = \{CD \rightarrow E\}$$

b. What's the strongest normal form of  $R_3$  and  $R_2$  respectively?

**The strongest normal form of  $R_3$  is potentially 1NF ( $R_3$  violates 2NF due to  $A \rightarrow B$  but  $A$  is a proper subset of the key  $\{A, D\}$ ) and  $R_2$  is BCNF (since there is only one dependency  $CD \rightarrow E$ )**

c. Is this decomposition lossless join?

**Yes, since the  $R_3 \cap R_2 = \{C, D\}$  and  $\{C, D\}$  is a key for  $R_2$**

d. Is this decomposition dependency preserving?

**Yes (it is easy to check that  $(F_{R_3} \cup F_{R_2})^+ = F^+$ )**

Let relation  $R(A, B, C, D, E)$  have a functional dependency set  $F=\{A \rightarrow B, B \rightarrow C, CD \rightarrow E\}$  (same as before).

3. Suppose we decompose  $R$  into  $R_4(A, B)$ ,  $R_5(B, C)$ ,  $R_2(C, D, E)$ .

a. Compute the local dependencies in  $F_{R_4}$ ,  $F_{R_5}$  and  $F_{R_2}$ .

$$F_{R_4} = \{A \rightarrow B\}$$

$$F_{R_5} = \{B \rightarrow C\}$$

$$F_{R_2} = \{CD \rightarrow E\}$$

b. What's the strongest normal form of  $R_4$ ,  $R_5$ , and  $R_2$  respectively?

**The strongest normal form of  $R_4$  is BCNF (since there is only one dependency  $A \rightarrow B$ ),  $R_5$  is BCNF (since there is only one dependency  $B \rightarrow C$ ),  $R_2$  is BCNF (since there is only one dependency  $CD \rightarrow E$ )**

c. Is this decomposition lossless join?

**No, since the  $R_5 \cap R_2 = C$  but  $C$  is a key for neither  $R_5$  nor  $R_2$**

d. Is this decomposition dependency preserving?

**Yes (it is easy to check that  $(F_{R_3} \cup F_{R_2})^+ = F^+$ )**

4. Suppose we decompose  $R$  into  $R_6(A, B, D)$ ,  $R_7(A, C, D, E)$ .

a. Compute the local dependencies in  $F_{R_6}$  and  $F_{R_7}$ .

$$F_{R_6} = \{A \rightarrow B\}$$

$$F_{R_7} = \{A \rightarrow C, CD \rightarrow E\}$$

b. What's the strongest normal form of  $R_6$  and  $R_7$  respectively?

**The strongest normal form of  $R_6$  is potentially 1NF (since  $\{A, D\}$  is the set of prime attributes and we have  $A \rightarrow B$  which is a 2NF violation),  $R_7$  is potentially 1NF (since  $\{A, D\}$  is the set of prime attributes and we have  $A \rightarrow C$  which is a 2NF violation)**

c. Is this decomposition lossless join?

**Yes, since the  $R_6 \cap R_7 = \{A, D\}$  and  $\{A, D\}$  is a key for  $R_6$  (and  $R_7$ )**

d. Is this decomposition dependency preserving?

**No (it is easy to check that  $(F_{R_6} \cup F_{R_7})^+ \neq F^+$  by noting that the dependency  $B \rightarrow C$  is missing in  $(F_{R_6} \cup F_{R_7})^+$  whereas  $B \rightarrow C$  is present in  $F^+$ )**